

# NANOSCALE ELASTIC-PROPERTY MAPPING WITH CONTACT-RESONANCE-FREQUENCY AFM

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# Introduction and Motivation

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- Mechanical properties are critical in many applications
  - predictive modeling of complex systems
  - performance and reliability
- Increasing need for information on the *nanoscale*
- Existing methods not optimal (too big, destructive, qualitative, ...)
- *Imaging* – visualization – increasingly important
  - multiple materials integrated at micro-, nanoscale
  - failure often due to local property variations

## *Objective:*

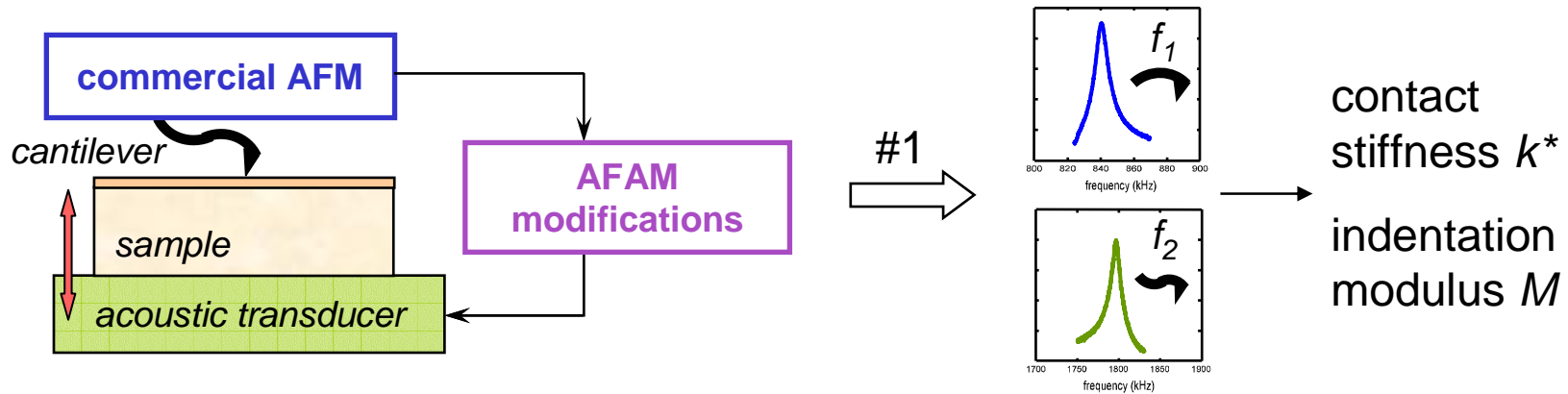
Develop AFM methods for quantitative elastic-property imaging

Approach based on atomic force acoustic microscopy (AFAM)



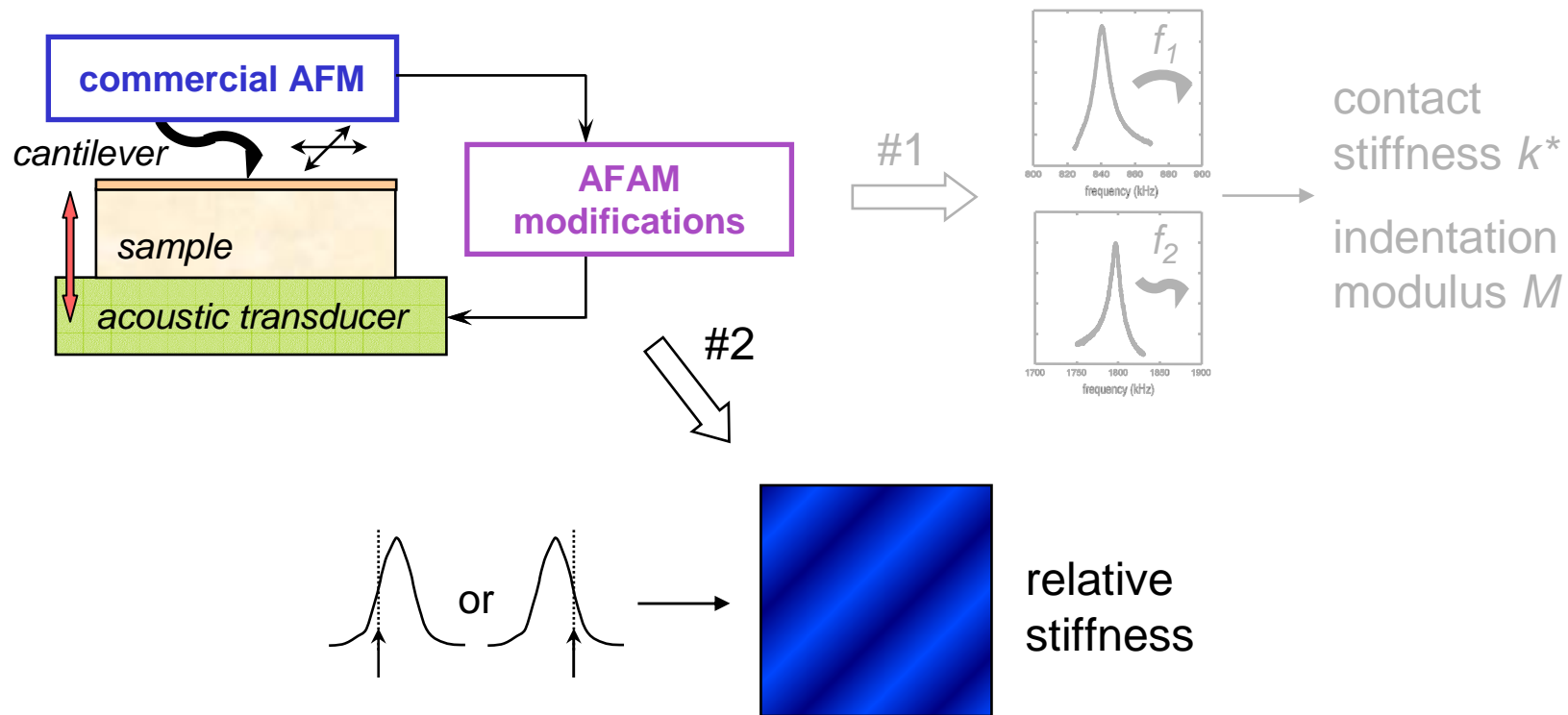
# Nanoscale Elastic Measurements with AFAM

1. sweep frequency at fixed tip position → quantitative point measurement



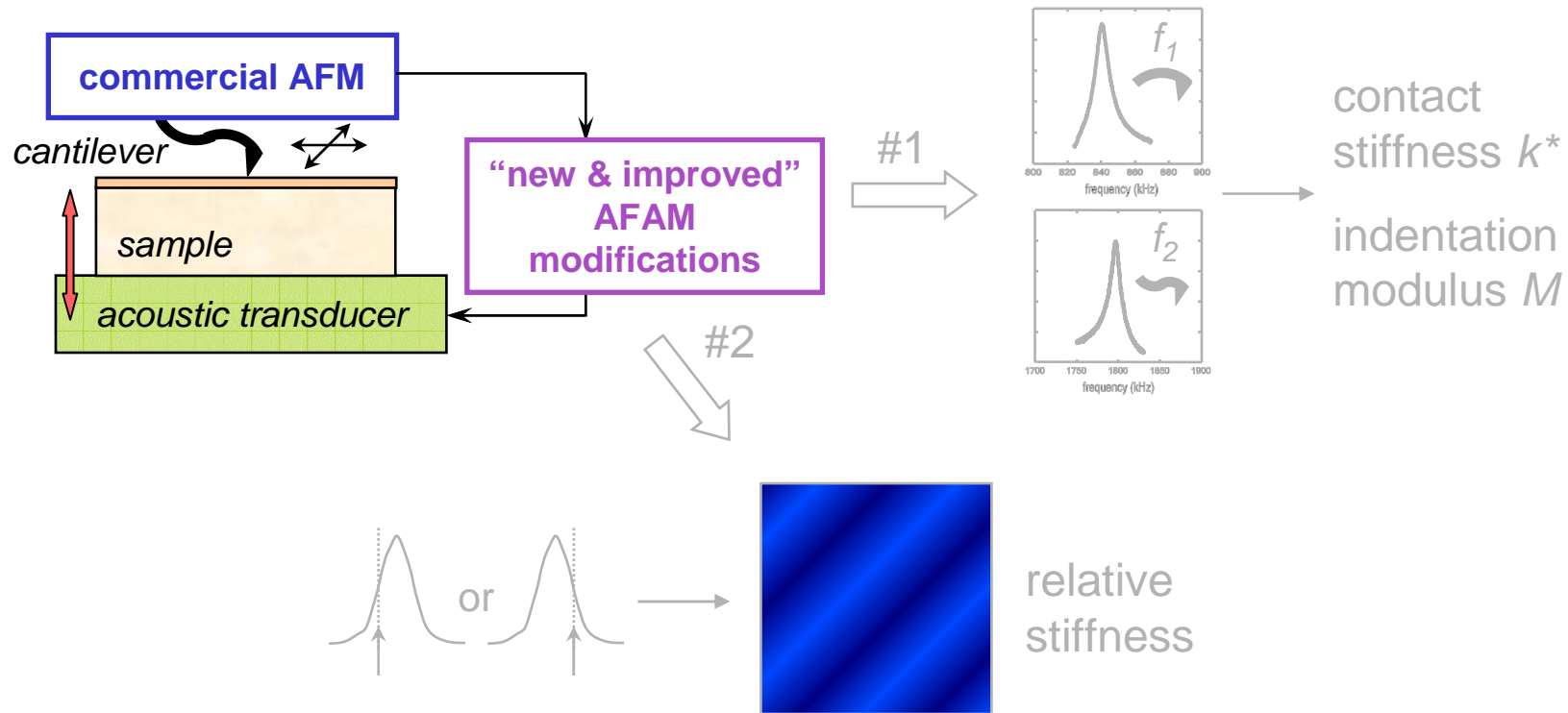
# Nanoscale Elastic Measurements with AFAM

1. sweep frequency at fixed tip position → quantitative point measurement  
OR 2. scan tip position at fixed frequency → qualitative image



# Nanoscale Elastic Measurements with AFAM

1. sweep frequency at fixed tip position → quantitative point measurement
- OR 2. scan tip position at fixed frequency → qualitative image

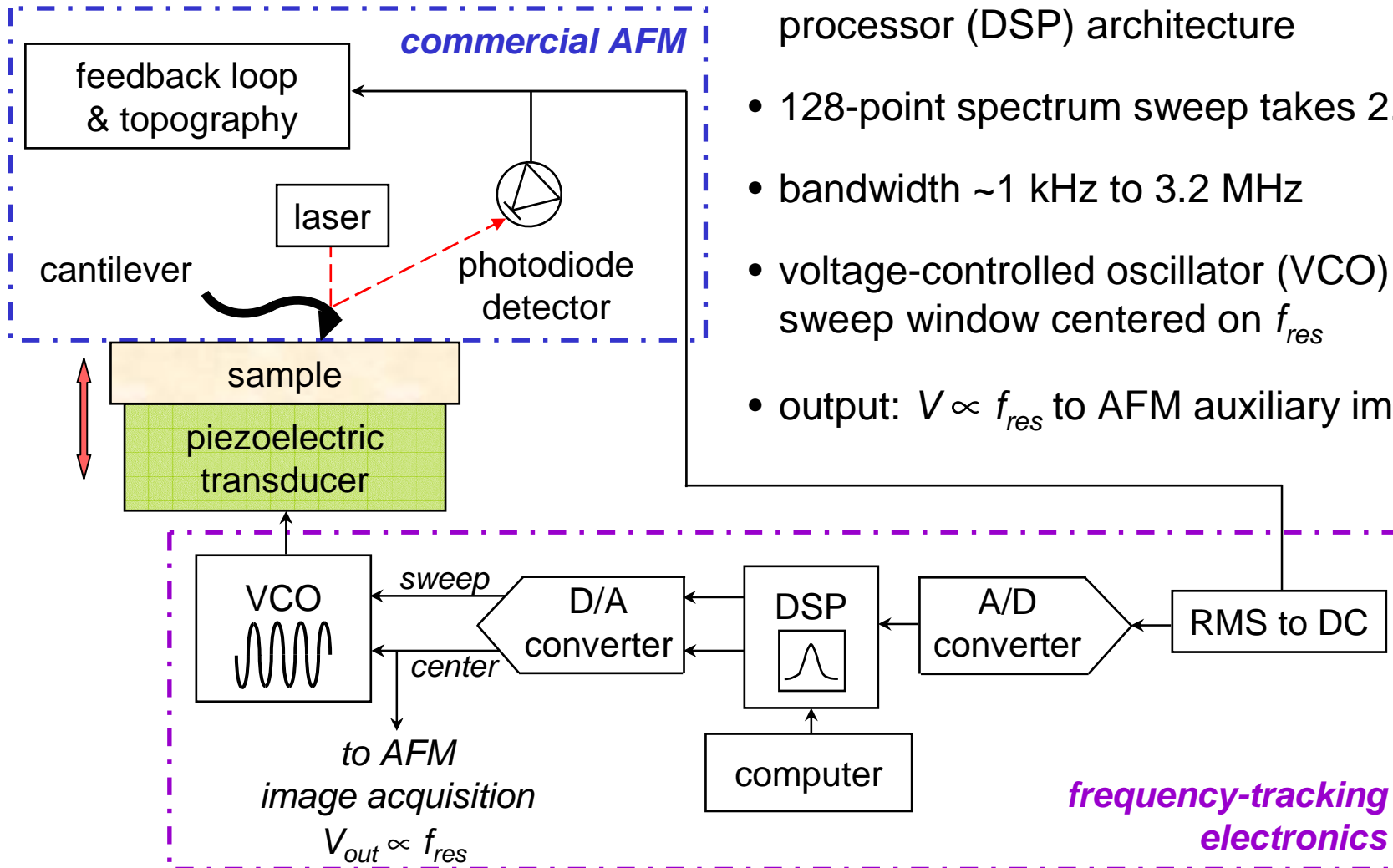


***NEXT: Quantitative imaging of elastic properties***

***CHALLENGE: Do it fast!***

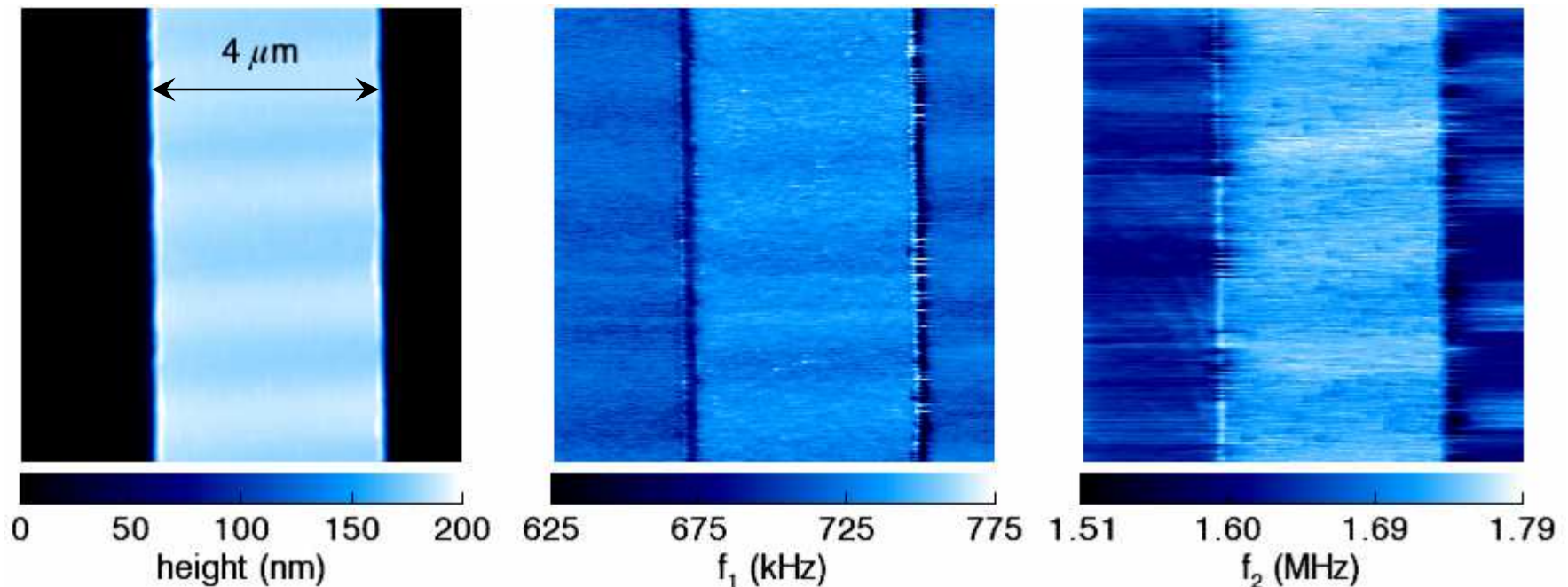
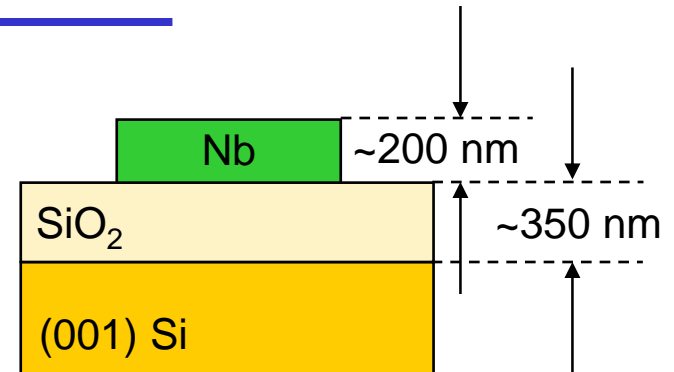
# Contact-Resonance Frequency Imaging

- electronics to track resonant frequency  $f_{res}$
- 32-bit, floating-point digital signal processor (DSP) architecture
- 128-point spectrum sweep takes 2.7 ms
- bandwidth  $\sim 1$  kHz to 3.2 MHz
- voltage-controlled oscillator (VCO) keeps sweep window centered on  $f_{res}$
- output:  $V \propto f_{res}$  to AFM auxiliary image port



# Examples of Frequency Images

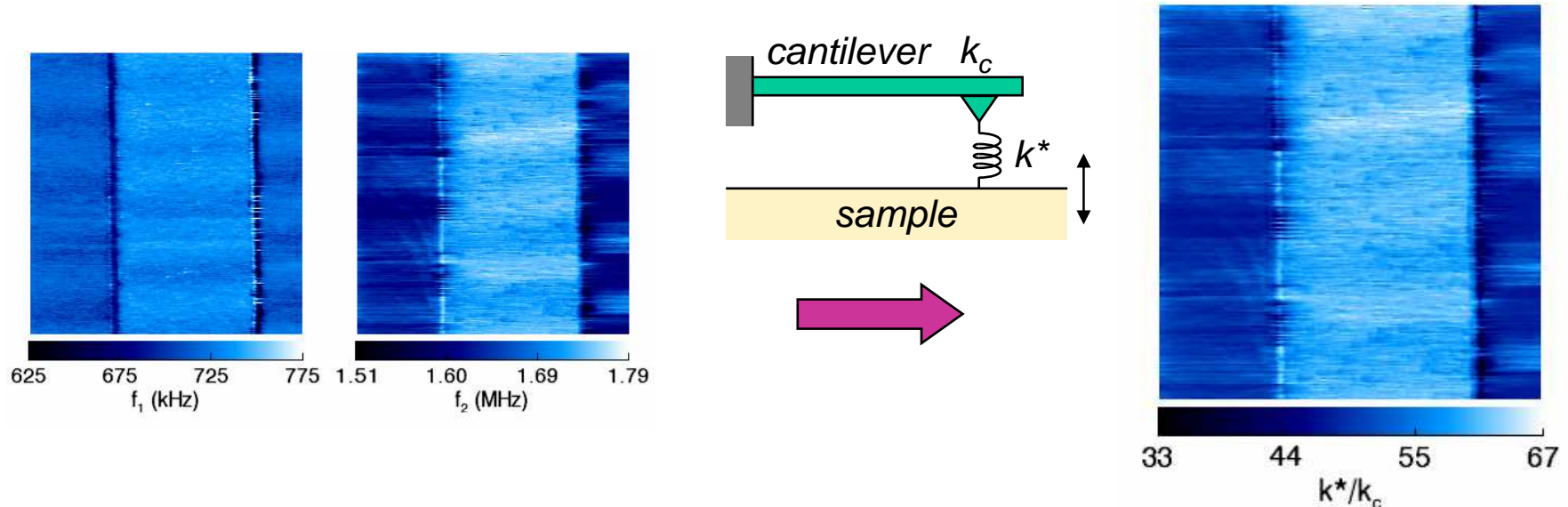
- 4  $\mu\text{m}$  niobium “wire” on silica blanket film
- Image lowest 2 flexural (bending) modes
- ~22 minutes for each 256 x 256 image



cantilever used (vendor specs):  
 $k_c = 47 \text{ N/m}$ ,  $L = 225 \mu\text{m}$ ,  $W = 34 \mu\text{m}$ ,  $t = 7.1 \mu\text{m}$

# Using Resonant-Frequency Images To Obtain Elastic-Property Information

- Contact stiffness: calculate  $k^*/k_c$  from  $f_1$  and  $f_2$  with beam-dynamics model



- Elastic modulus: requires data from reference material

$$E_{sample}^* = E_{ref}^* \left( \frac{k_{sample}^* / k_c}{k_{ref}^* / k_c} \right)^n$$

$n=1$  flat punch     $n=3/2$  Hertzian

$$\frac{1}{E^*} = \frac{1}{M_{tip}} + \frac{1}{M_{sample}}$$

$M_{tip} = 165 \text{ GPa for Si } \langle 100 \rangle$

$$M = \frac{E}{1 - \nu^2}$$

(isotropic)

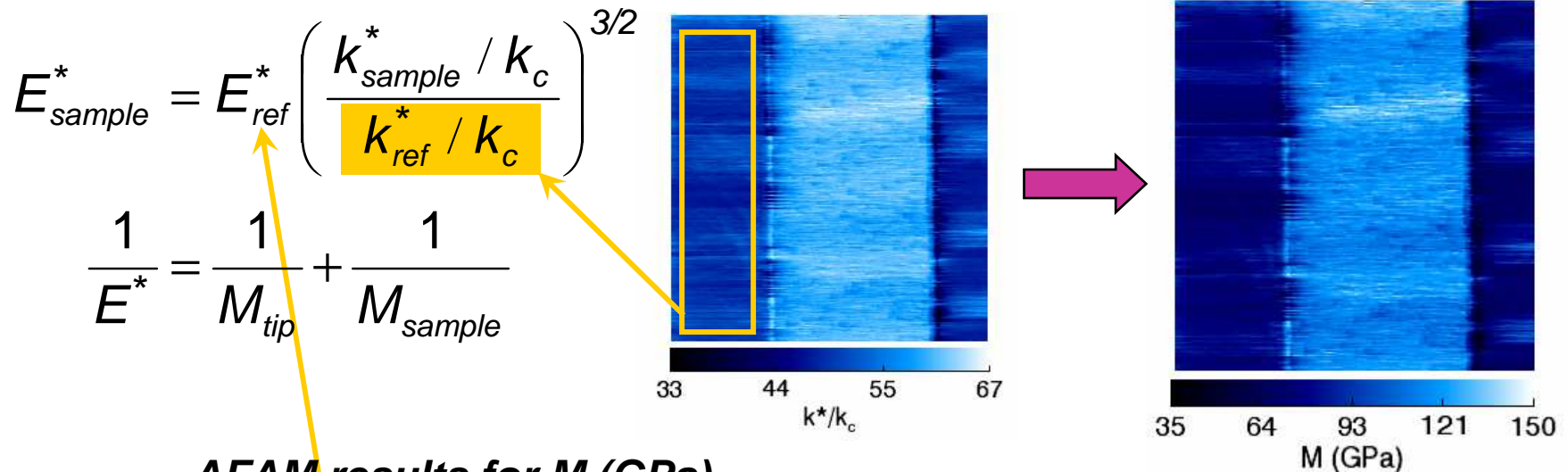
$E$  = Young's modulus

$\nu$  = Poisson's ratio



# Calculating Modulus Maps from Contact-Stiffness Images

- Assume Hertzian contact mechanics
- Use “self-calibrating” method based on fixed-point measurements



**AFAM results for  $M$  (GPa)**

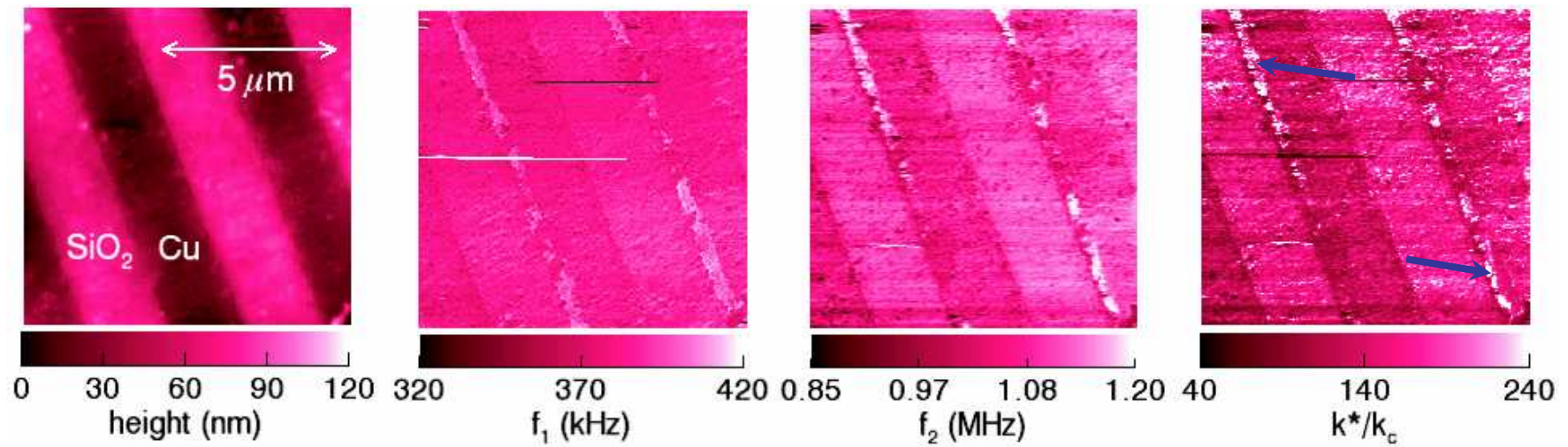
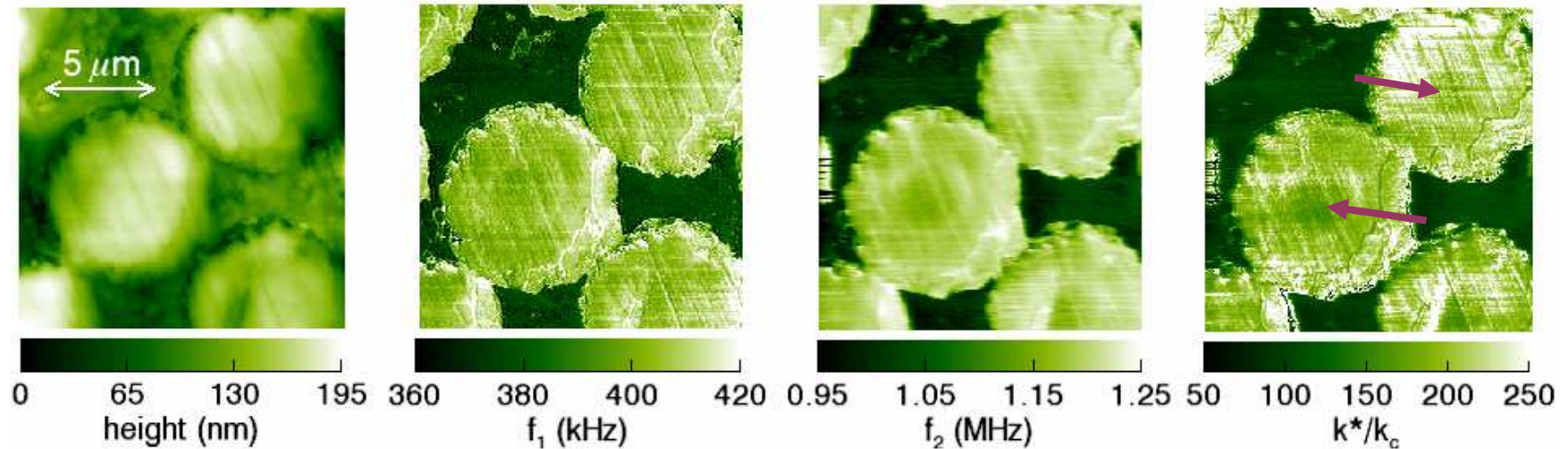
method	film material	
	SiO <sub>2</sub>	Nb
fixed-point	75.1 ± 10.0	112.7 ± 15.0
image	75.5 ± 7.1	118.5 ± 7.1
literature	72-77	116-133

reference: fused silica,  $M = 74.9$  GPa

*Image values for  $M$  agree well with other data*

## Additional Flexural-Mode Images

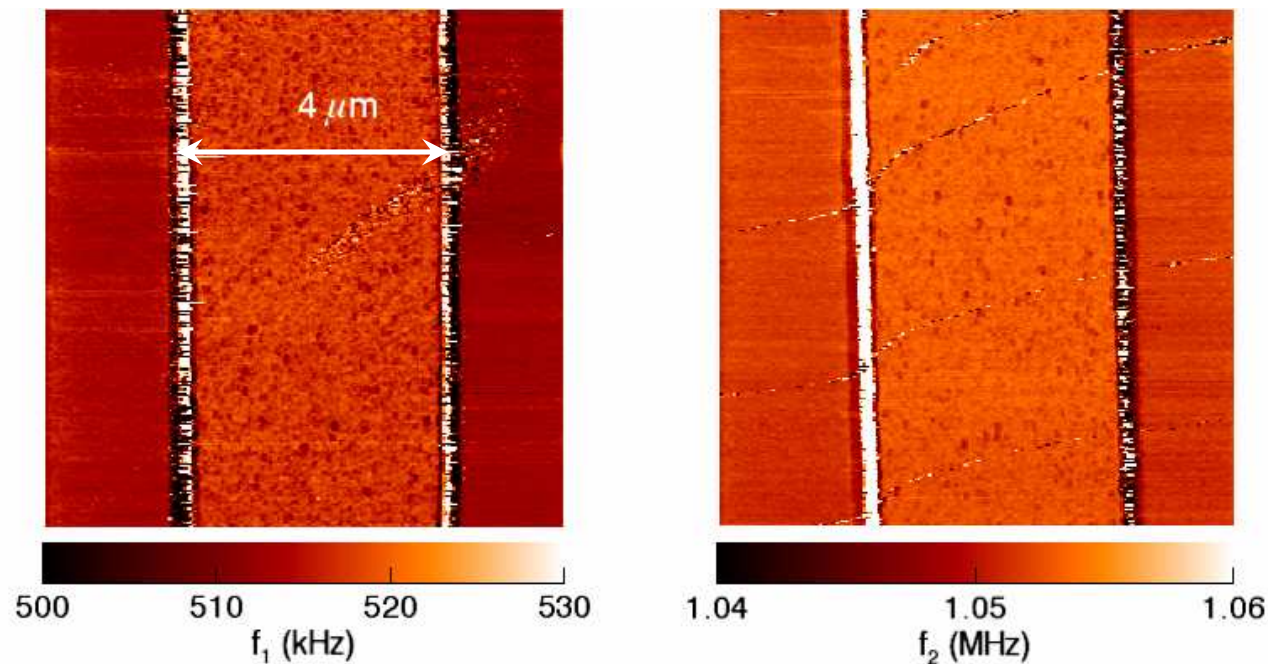
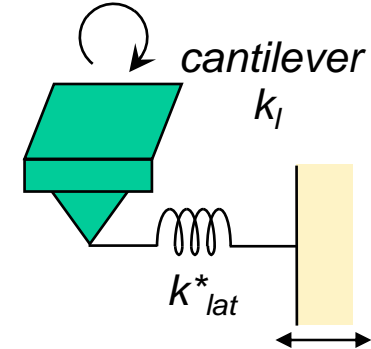
*epoxy/glass composite*



*$\text{Cu}/\text{SiO}_2$  microelectronic test structure*

# Torsional Mode Images

- Detect torsional modes with left-to-right photodiode signal
- Obtain lateral (horizontal) contact stiffness  $k_{lat}^*$
- Yields information about shear modulus  $G = \frac{E}{2(1+\nu)}$
- Next: develop methods to calculate  $k_{lat}^*$ ,  $G$  from  $f_1$  and  $f_2$



cantilever used (vendor specs):

$$k_c = 1 \text{ N/m}, L = 448 \text{ } \mu\text{m}, W = 51 \text{ } \mu\text{m}, t = 3.5 \text{ } \mu\text{m}$$



# Summary and Conclusions

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- AFAM uses contact-resonance modes of the AFM cantilever to nondestructively measure elastic properties.
- We have developed frequency-tracking electronics to obtain *nanoscale elastic-property maps* with AFAM.
- Flexural- and torsional-mode frequency images were shown to demonstrate the basic approach.
- Contact-stiffness images using flexural-mode images yield values of  $M$  in agreement with other results.
- Several issues (contact mechanics, calibration, etc.) must be further addressed for truly quantitative imaging.

